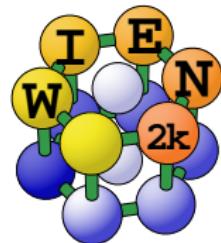


# Methods available in WIEN2k for the treatment of exchange and correlation effects

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24th WIEN2k workshop, 18-22 September 2017  
Vienna University of Technology, Vienna, Austria



# Outline of the talk

- ▶ Introduction
- ▶ Semilocal functionals:
  - ▶ GGA and MGGA
  - ▶ mBJ potential (for band gap)
  - ▶ Input file case.in0
- ▶ Methods for van der Waals systems:
  - ▶ DFT-D3
  - ▶ Nonlocal functionals
- ▶ On-site methods for strongly correlated  $d$  and  $f$  electrons:
  - ▶ DFT+ $U$
  - ▶ Hybrid functionals
- ▶ Hybrid functionals

# Total energy in Kohn-Sham DFT<sup>1</sup>

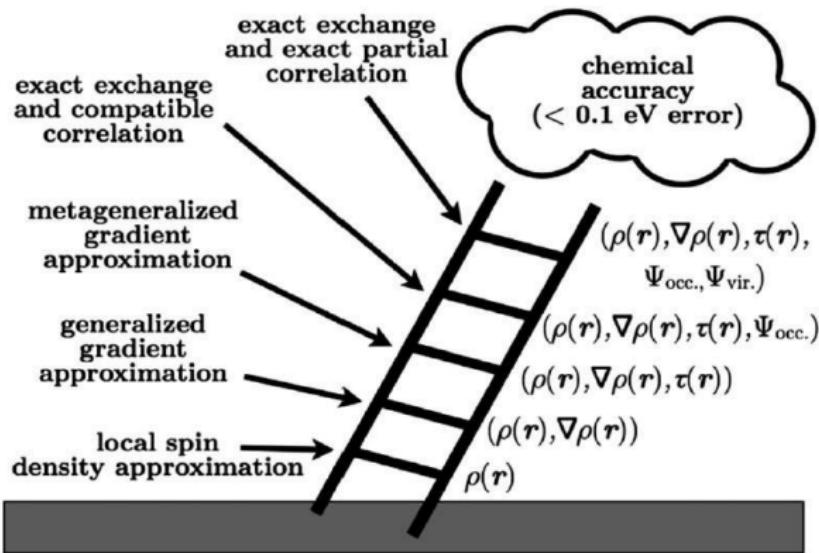
$$E_{\text{tot}} = \underbrace{\frac{1}{2} \sum_i \int |\nabla \psi_i(\mathbf{r})|^2 d^3 r}_{T_s} + \underbrace{\frac{1}{2} \int \int \frac{\rho(\mathbf{r})\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d^3 r d^3 r'}_{E_{ee}} + \underbrace{\int v_{\text{en}}(\mathbf{r})\rho(\mathbf{r})d^3 r}_{E_{en}}$$
$$+ \underbrace{\frac{1}{2} \sum_{\substack{A,B \\ A \neq B}} \frac{Z_A Z_B}{|\mathbf{R}_A - \mathbf{R}_B|}}_{E_{nn}} + E_{\text{xc}}$$

- ▶  $T_s$  : kinetic energy of the non-interacting electrons
- ▶  $E_{ee}$  : repulsive electron-electron electrostatic Coulomb energy
- ▶  $E_{en}$  : attractive electron-nucleus electrostatic Coulomb energy
- ▶  $E_{nn}$  : repulsive nucleus-nucleus electrostatic Coulomb energy
- ▶  $E_{\text{xc}} = E_x + E_c$  : exchange-correlation energy  
Approximations for  $E_{\text{xc}}$  have to be used in practice  
 $\Rightarrow$  The reliability of the results depends mainly on  $E_{\text{xc}}$

<sup>1</sup> W. Kohn and L. J. Sham, Phys. Rev. **140**, A1133 (1965)

# Approximations for $E_{xc}$ (Jacob's ladder<sup>1</sup>)

$$E_{xc} = \int \epsilon_{xc}(\mathbf{r}) d^3r$$



The accuracy, but also the computational cost, increase when climbing up the ladder

<sup>1</sup> J. P. Perdew et al., J. Chem. Phys. 123, 062201 (2005)

# Kohn-Sham Schrödinger equations

Minimization of  $E_{\text{tot}}$  leads to

$$\left( -\frac{1}{2} \nabla^2 + v_{\text{ee}}(\mathbf{r}) + v_{\text{en}}(\mathbf{r}) + \hat{v}_{\text{xc}}(\mathbf{r}) \right) \psi_i(\mathbf{r}) = \epsilon_i \psi_i(\mathbf{r})$$

Two types of  $\hat{v}_{\text{xc}}$ :

- ▶ Multiplicative:  $\hat{v}_{\text{xc}} = \delta E_{\text{xc}} / \delta \rho = v_{\text{xc}}$  (KS method)
  - ▶ LDA
  - ▶ GGA
- ▶ Non-multiplicative:  $\hat{v}_{\text{xc}} = (1/\psi_i) \delta E_{\text{xc}} / \delta \psi_i^* = v_{\text{xc},i}$  (generalized KS<sup>1</sup>)
  - ▶ Hartree-Fock
  - ▶ LDA+ $U$
  - ▶ Hybrid (mixing of GGA and Hartree-Fock)
  - ▶ MGGA
  - ▶ Self-interaction corrected (Perdew-Zunger)

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<sup>1</sup> A. Seidl et al., Phys. Rev. B 53, 3764 (1996)

## Semilocal functionals: GGA

$$\epsilon_{xc}^{\text{GGA}}(\rho, \nabla\rho) = \epsilon_x^{\text{LDA}}(\rho) F_{\text{xc}}(r_s, s)$$

where  $F_{\text{xc}}$  is the enhancement factor and

$$r_s = \frac{1}{\left(\frac{4}{3}\pi\rho\right)^{1/3}} \quad (\text{Wigner-Seitz radius})$$

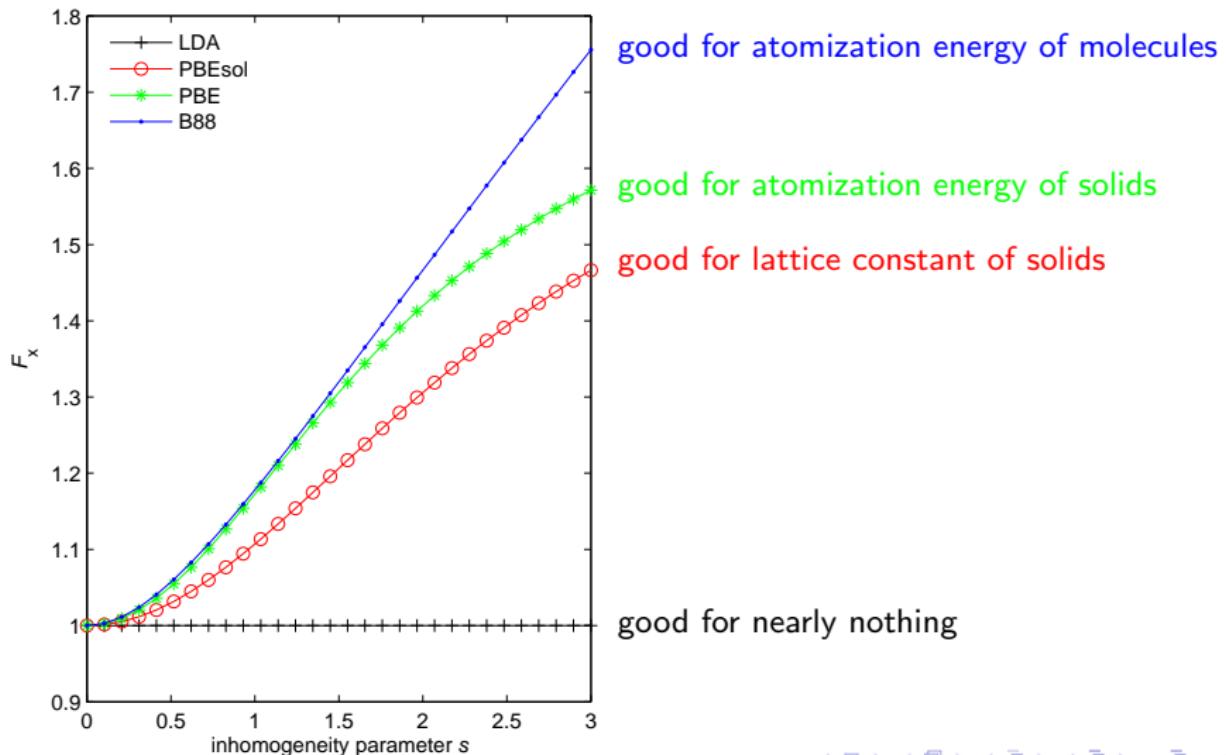
$$s = \frac{|\nabla\rho|}{2(3\pi^2)^{1/3} \rho^{4/3}} \quad (\text{inhomogeneity parameter})$$

There are two types of GGA:

- ▶ **Semi-empirical**: contain parameters fitted to accurate (i.e., experimental) data.
- ▶ **Ab initio**: All parameters were determined by using mathematical conditions obeyed by the exact functional.

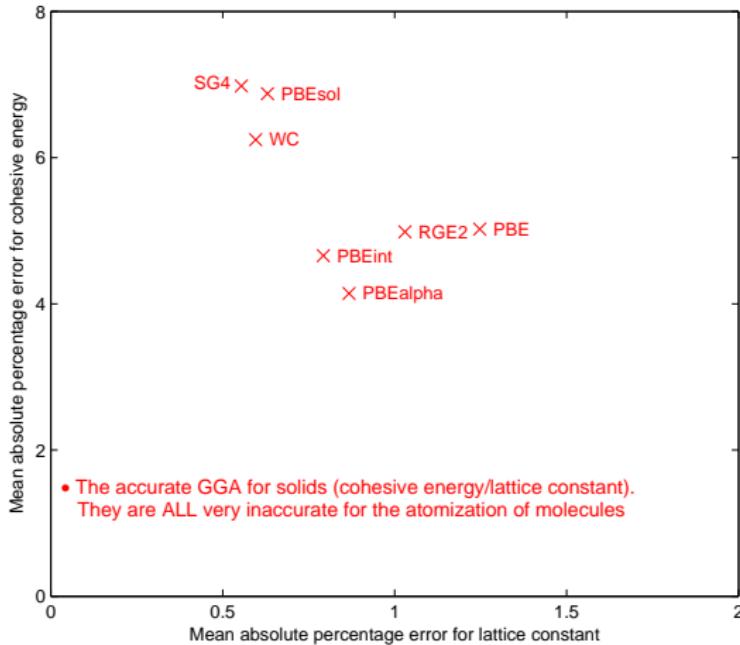
# Semilocal functionals: trends with GGA

Exchange enhancement factor  $F_x(s) = \epsilon_x^{\text{GGA}} / \epsilon_x^{\text{LDA}}$



# Construction of an universal GGA: A failure

## Test of functionals on 44 solids<sup>1</sup>



<sup>1</sup> F. Tran et al., J. Chem. Phys. 144, 204120 (2016)

# Semilocal functionals: meta-GGA

$$\epsilon_{\text{xc}}^{\text{MGGA}}(\rho, \nabla\rho, t) = \epsilon_{\text{xc}}^{\text{LDA}}(\rho) F_{\text{xc}}(r_s, s, \alpha)$$

- ▶  $\alpha = \frac{t - t_{\text{W}}}{t_{\text{TF}}}$ 
  - ▶  $\alpha = 1$  (region of constant electron density)
  - ▶  $\alpha = 0$  (in one- and two-electron regions very close and very far from nuclei)
  - ▶  $\alpha \gg 1$  (region between closed shell atoms)

⇒ MGGA functionals are more flexible

Example: **SCAN<sup>1</sup>** is

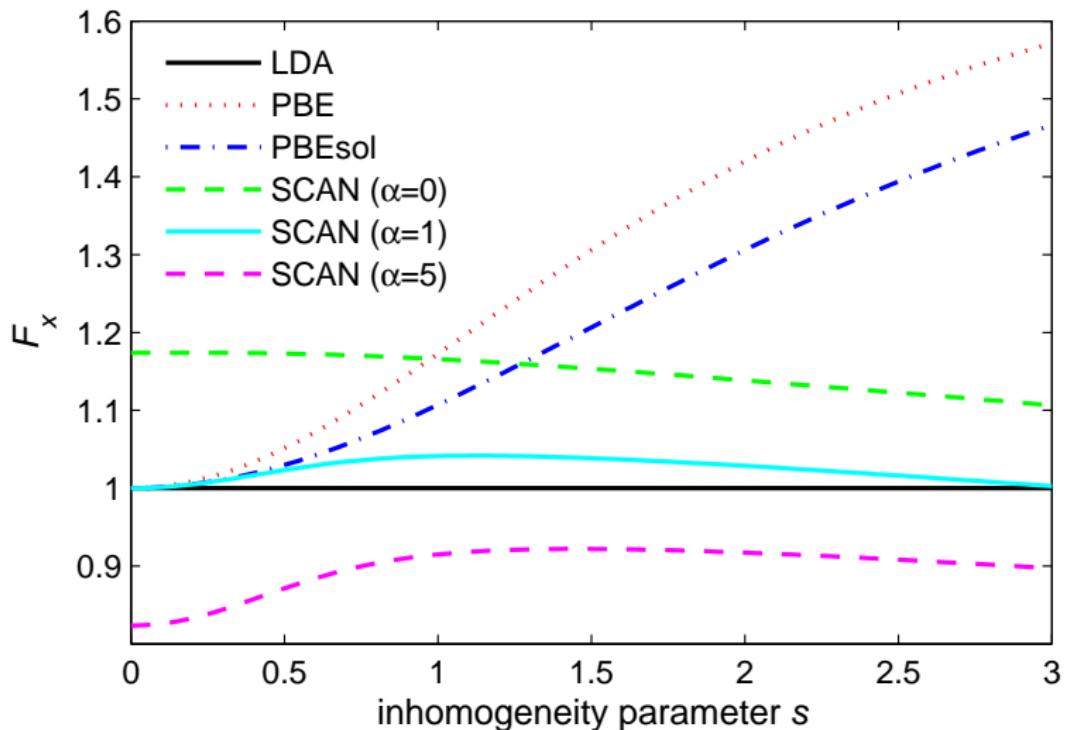
- ▶ as good as the best GGA for atomization energies of molecules
- ▶ as good as the best GGA for lattice constant of solids

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<sup>1</sup> J. Sun et al., Phys. Rev. Lett. 115, 036402 (2015)

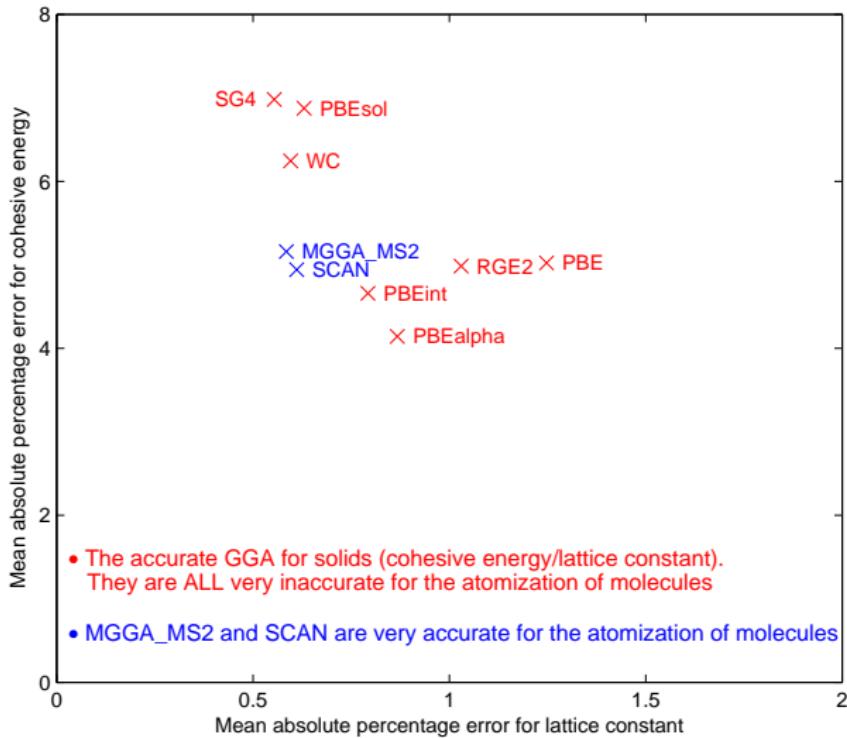
# Semilocal functionals: meta-GGA

$$F_x(s, \alpha) = \epsilon_x^{\text{MGGA}} / \epsilon_x^{\text{LDA}}$$



# Semilocal functionals: MGGA\_MS2 and SCAN

## Test of functionals on 44 solids<sup>1</sup>



<sup>1</sup> F. Tran et al., J. Chem. Phys. 144, 204120 (2016)

## Semilocal potential for band gap: modified Becke-Johnson

- ▶ Standard LDA and GGA functionals underestimate the band gap
- ▶ Hybrid and  $GW$  are much more accurate, but also much more expensive
- ▶ A cheap alternative is to use the modified Becke-Johnson (mBJ) potential:<sup>1</sup>

$$v_x^{\text{mBJ}}(\mathbf{r}) = c v_x^{\text{BR}}(\mathbf{r}) + (3c - 2) \frac{1}{\pi} \sqrt{\frac{5}{6}} \sqrt{\frac{t(\mathbf{r})}{\rho(\mathbf{r})}}$$

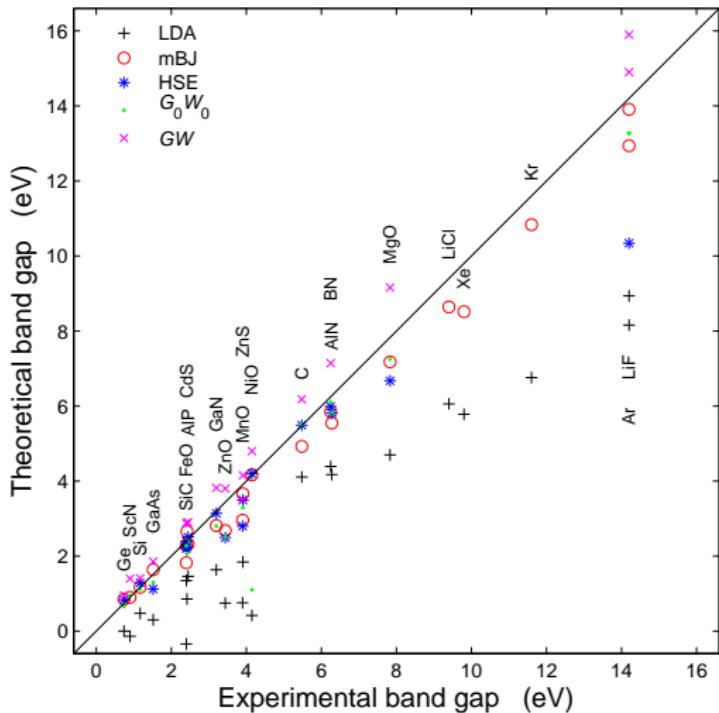
where  $v_x^{\text{BR}}$  is the Becke-Roussel potential,  $t$  is the kinetic-energy density and  $c$  is given by

$$c = \alpha + \beta \left( \frac{1}{V_{\text{cell}}} \int_{\text{cell}} \frac{|\nabla \rho(\mathbf{r})|}{\rho(\mathbf{r})} d^3 r \right)^p$$

mBJ is a MGGA potential

<sup>1</sup>F. Tran and P. Blaha, Phys. Rev. Lett. 102, 226401 (2009)

# Band gaps with mBJ



See also F. Tran and P. Blaha, J. Phys. Chem. A 121, 3318 (2017)

# How to run a calculation with the mBJ potential?

1. init\_lapw (choose LDA or PBE)
2. init\_mbj\_lapw (create/modify files)
  - 2.1 automatically done: `case.in0` modified and `case.inm_vresp` created
  - 2.2 `run(sp)_lapw -i 1 -NI` (creates `case.r2v` and `case.vrespm`)
  - 2.3 save\_lapw
3. init\_mbj\_lapw and choose one of the parametrizations:
  - 0: Original mBJ values<sup>1</sup>
  - 1: New parametrization<sup>2</sup>
  - 2: New parametrization for semiconductors<sup>2</sup>
  - 3: Original BJ potential<sup>3</sup>
4. run(sp)\_lapw ...

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<sup>1</sup> F. Tran and P. Blaha, Phys. Rev. Lett. **102**, 226401 (2009)

<sup>2</sup> D. Koller *et al.*, Phys. Rev. B **85**, 155109 (2012)

<sup>3</sup> A. D. Becke and E. R. Johnson, J. Chem. Phys. **124**, 221101 (2006)

# Input file case.in0: keywords for the xc-functional

The functional is specified at the 1st line of `case.in0`. Three different ways:

1. Specify a global keyword for  $E_x$ ,  $E_c$ ,  $v_x$ ,  $v_c$ :
  - ▶ TOT `XC_NAME`
2. Specify a keyword for  $E_x$ ,  $E_c$ ,  $v_x$ ,  $v_c$  individually:
  - ▶ TOT `EX_NAME1 EC_NAME2 VX_NAME3 VC_NAME4`
3. Specify keywords to use functionals from **LIBXC**<sup>1</sup>:
  - ▶ TOT `XC_TYPE_X_NAME1 XC_TYPE_C_NAME2`
  - ▶ TOT `XC_TYPE_XC_NAME`

where **TYPE** is the family name: **LDA**, **GGA** or **MGGA**

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<sup>1</sup> M. A. L. Marques et al., Comput. Phys. Commun. **183**, 2272 (2012)

<http://www.tddft.org/programs/octopus/wiki/index.php/Libxc>

## Input file case.in0: examples

- ▶ PBE:

TOT XC\_PBE

or

TOT EX\_PBE EC\_PBE VX\_PBE VC\_PBE

or

TOT XC\_GGA\_X\_PBE XC\_GGA\_C\_PBE

- ▶ mBJ (with LDA for the xc-energy):

TOT XC\_MBJ

- ▶ MGGA\_MS2:

TOT XC\_MGGA\_MS  $\underbrace{0.504 \ 0.14601 \ 4.0}_{\kappa, c, b}$

All available functionals are listed in tables of the user's guide and in  
\$WIENROOT/SRC\_lapw0/xc\_funcs.h for **LIBXC** (if installed)

# Methods for van der Waals systems

Problem with semilocal and hybrid functionals:

- ▶ They do not include London dispersion interactions  $\Rightarrow$   
Results are very often qualitatively wrong for van der Waals systems

Two types of dispersion terms added to the DFT total energy:

- ▶ Pairwise term (cheap)<sup>1</sup>:

$$E_{c,\text{disp}}^{\text{PW}} = - \sum_{A < B} \sum_{n=6,8,10,\dots} f_n^{\text{damp}}(R_{AB}) \frac{C_n^{AB}}{R_{AB}^n}$$

- ▶ Nonlocal term (more expensive than semilocal)<sup>2</sup>:

$$E_{c,\text{disp}}^{\text{NL}} = \frac{1}{2} \int \int \rho(\mathbf{r}_1) \Phi(\mathbf{r}_1, \mathbf{r}_2) \rho(\mathbf{r}_2) d^3 r_1 d^3 r_2$$

---

<sup>1</sup> S. Grimme, J. Comput. Chem. **25**, 1463 (2004)

<sup>2</sup> M. Dion et al., Phys. Rev. Lett. **92**, 246401 (2004)

# DFT-D3 pairwise method<sup>1</sup>

- ▶ Features:
  - ▶ Cheap
  - ▶  $C_n^{AB}$  depend on positions of the nuclei (via coordination number)
  - ▶ Energy and forces (minimization of internal parameters)
  - ▶ 3-body term available (more important for solids than molecules)
- ▶ Installation:
  - ▶ Not included in WIEN2k
  - ▶ Download and compile the DFTD3 package from  
<https://www.chemie.uni-bonn.de/pctc/mulliken-center/software/dft-d3/>  
copy the `dftd3` executable in `$WIENROOT`
- ▶ Usage:
  - ▶ Input file `case.indftd3` (if not present a default one is copied automatically by `x_lapw`)
  - ▶ `run(sp)_lapw -dftd3 ...`
  - ▶ `case.scfdftd3` is included in `case.scf`

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<sup>1</sup> S. Grimme et al., J. Chem. Phys. 132, 154104 (2010)

## DFT-D3 method: input file case.indftd3

Default (and recommended) input file:

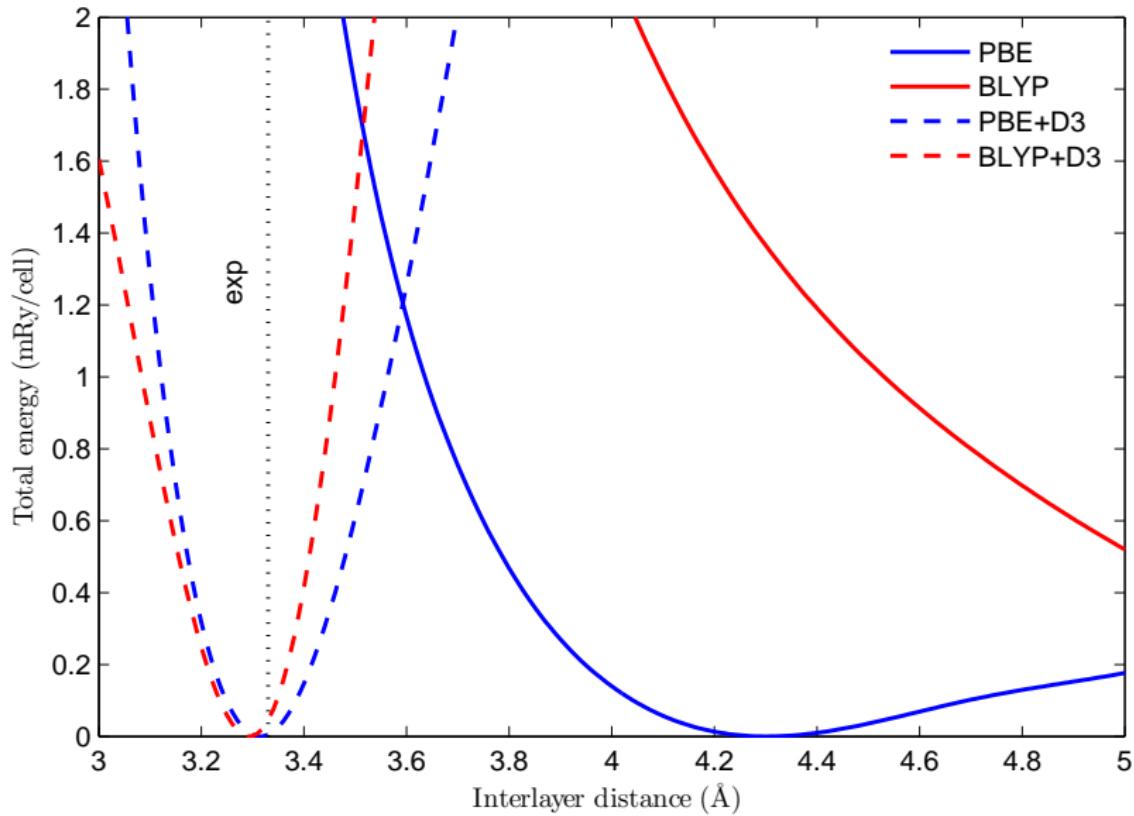
---

<b>method</b>	<b>bj</b>	damping function $f_n^{\text{damp}}$
<b>func</b>	<b>default</b>	the one in case.in0*
<b>grad</b>	<b>yes</b>	forces
<b>pbc</b>	<b>yes</b>	periodic boundary conditions
<b>abc</b>	<b>yes</b>	3-body term
<b>cutoff</b>	<b>95</b>	interaction cutoff
<b>cnthr</b>	<b>40</b>	coordination number cutoff
<b>num</b>	<b>no</b>	numerical gradient

---

\***default** will work for PBE, PBEsol, BLYP and TPSS. For other functionals, the functional name has to be specified (see dftd3.f of DFTD3 package)

# DFT-D3 method: hexagonal BN<sup>1</sup>



<sup>1</sup> F. Tran et al., J. Chem. Phys. 144, 204120 (2016)

# Nonlocal vdW functionals

$$E_{c,\text{disp}}^{\text{NL}} = \frac{1}{2} \int \int \rho(\mathbf{r}_1) \Phi(\mathbf{r}_1, \mathbf{r}_2) \rho(\mathbf{r}_2) d^3 r_1 d^3 r_2$$

Kernels  $\Phi$  proposed in the literature:

- ▶ **DRSLL**<sup>1</sup> (vdW-DF1, optB88-vdW, vdW-DF-cx0, . . .):
  - ▶ Derived from ACFDT
  - ▶ Contains no adjustable parameter
- ▶ **LMKLL**<sup>2</sup> (vdW-DF2, rev-vdW-DF2):
  - ▶  $Z_{ab}$  in DRSLL multiplied by 2.222
- ▶ **rVV10**<sup>3,4</sup>:
  - ▶ Different analytical form as DRSLL
  - ▶ Parameters:  $b = 6.3$  and  $C = 0.0093$
- ▶ **rVV10L**<sup>5</sup>:
  - ▶ Parameters:  $b = 10.0$  and  $C = 0.0093$

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<sup>1</sup> M. Dion *et al.*, Phys. Rev. Lett. **92**, 246401 (2004)

<sup>2</sup> K. Lee *et al.*, Phys. Rev. B **82**, 081101(R) (2010)

<sup>3</sup> O. A. Vydrov and T. Van Voorhis, J. Chem. Phys. **133**, 244103 (2010)

<sup>4</sup> R. Sabatini *et al.*, Phys. Rev. B **87**, 041108(R) (2013)

<sup>5</sup> H. Peng and J. P. Perdew, Phys. Rev. B **95**, 081105(R) (2017)

# Nonlocal vdW functionals in WIEN2k<sup>1</sup>

## ► Features:

- ▶ Use the fast FFT-based method of Román-Pérez and Soler<sup>2</sup>:
  1.  $\rho$  is smoothed close to the nuclei (density cutoff  $\rho_c$ )  $\rightarrow \rho_s$ .  
The smaller  $\rho_c$  is, the smoother  $\rho_s$  is.
  2.  $\rho_s$  is expanded in plane waves in the whole unit cell.  
 $G_{\max}$  is the plane-wave cutoff of the expansion.
- ▶ Most vdW functionals from the literature are available (see user's guide)

## ► Usage:

- ▶ Input file `case.innlvdw` (`$WIENROOT/SRC_templates`)
- ▶ `run(sp)_lapw -nlvdw ...`
- ▶ `case.scfnlvdw` is included in `case.scf`

## ► Problem:

- ▶ **prepare\_xsf** may hang

---

<sup>1</sup>F. Tran *et al.*, Phys. Rev. B **96**, 054103 (2017)

<sup>2</sup>G. Román-Pérez and J. M. Soler, Phys. Rev. Lett. **103**, 096102 (2009)

## Nonlocal vdW functionals: the input file case.innlvdw

---

1	kernel type
-0.8491	parameters of the kernel
20	plane-wave expansion cutoff GMAX
0.3	density cutoff rhoc
T	calculation of the potential (T or F)

---

line 1 : "1" for DRSLL and LMKLL or "2" for rVV10

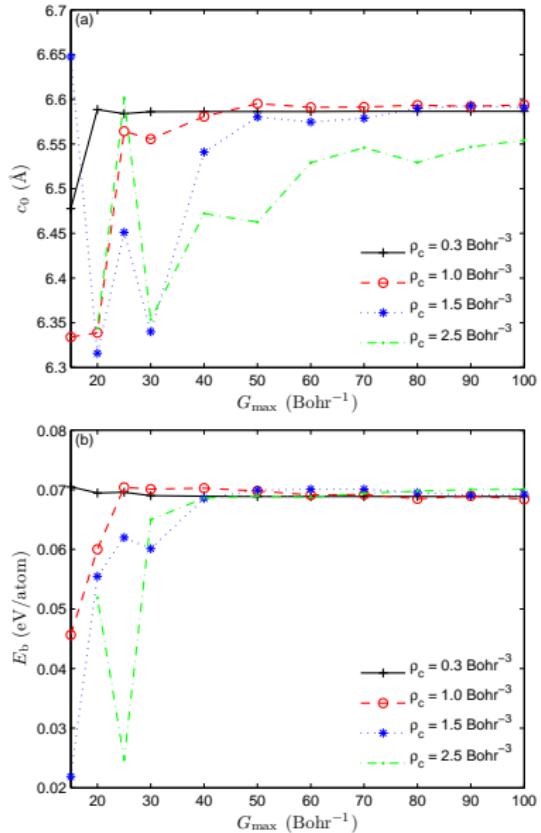
line 2 : "-0.8491" for DRSLL, "-1.887" for LMKLL or "6.3 0.0093" for rVV10

line 3 : Use  $G_{\max} = 25$  or 30 in case of numerical noise

line 4 : Eventually repeat with larger  $\rho_c$  (e.g. 0.6)

line 5 : Potential is necessary only for forces. Save computational time if set to "F"

# Nonlocal vdW functionals: convergence with $\rho_c$ and $G_{\max}$



# Strongly correlated electrons

Problem with semilocal functionals:

- ▶ They give qualitatively wrong results for solids which contain localized ***3d or 4f*** electrons
  - ▶ The band gap is too small (zero in FeO!)
  - ▶ The magnetic moment is too small (zero in  $\text{YBa}_2\text{Cu}_3\text{O}_6$ !)
  - ▶ Wrong electronic configuration

Why?

- ▶ The **strong on-site** correlations are not correctly accounted for by semilocal functionals.

(Partial) solution to the problem:

- ▶ Combine semilocal functionals with **Hartree-Fock** theory:
  - ▶ DFT+*U*
  - ▶ Hybrid

Even better:

- ▶ LDA+DMFT (DMFT codes using WIEN2k orbitals as input exist)

# On-site DFT+ $U$ and hybrid methods in WIEN2k

- ▶ For solids, the hybrid functionals are computationally **very expensive**.
- ▶ In WIEN2k the **on-site** DFT+ $U$ <sup>1</sup> and **on-site** hybrid<sup>2,3</sup> methods are available. These methods are approximations of the Hartree-Fock/hybrid methods
- ▶ Applied only inside atomic spheres of selected atoms and electrons of a given angular momentum  $\ell$ .

On-site methods → **As cheap as LDA/GGA.**

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<sup>1</sup>V. I. Anisimov *et al.*, Phys. Rev. B **44**, 943 (1991)

<sup>2</sup>P. Novák *et al.*, Phys. Stat. Sol. (b) **243**, 563 (2006)

<sup>3</sup>F. Tran *et al.*, Phys. Rev. B **74**, 155108 (2006)

# DFT+ $U$ and hybrid exchange-correlation functionals

The exchange-correlation functional is

$$E_{\text{xc}}^{\text{DFT}+U/\text{hybrid}} = E_{\text{xc}}^{\text{DFT}}[\rho] + E^{\text{onsite}}[n_{mm'}]$$

where  $n_{mm'}$  is the density matrix of the correlated electrons

- ▶ For DFT+ $U$  both exchange and Coulomb are corrected:

$$E^{\text{onsite}} = \underbrace{E_x^{\text{HF}} + E_{\text{Coul}}}_{\text{correction}} - \underbrace{E_x^{\text{DFT}} + E_{\text{Coul}}^{\text{DFT}}}_{\text{double counting}}$$

There are several versions of the double-counting term

- ▶ For the hybrid methods only exchange is corrected:

$$E^{\text{onsite}} = \underbrace{\alpha E_x^{\text{HF}}}_{\text{corr.}} - \underbrace{\alpha E_x^{\text{LDA}}}_{\text{d. count.}}$$

where  $\alpha$  is a parameter  $\in [0, 1]$

# How to run DFT+ $U$ and on-site hybrid calculations?

## 1. Create the input files:

- ▶ `case.inorb` and `case.indm` for DFT+ $U$
- ▶ `case.ineece` for on-site hybrid functionals (`case.indm` created automatically):

## 2. Run the job (can only be run with `runsp_lapw`):

- ▶ LDA+ $U$ : `runsp_lapw -orb ...`
- ▶ Hybrid: `runsp_lapw -eece ...`

For a calculation without spin-polarization ( $\rho_{\uparrow} = \rho_{\downarrow}$ ):

`runsp_c_lapw -orb/eece ...`

## Input file case.inorb

LDA+ $U$  applied to the  $4f$  electrons of atoms No. 2 and 4:

---

1 2 0	nmod, natorb, ipr
PRATT,1.0	mixmod, amix
2 1 3	iatom, nlorb, lorb
4 1 3	iatom, nlorb, lorb
1	nsic (LDA+U(SIC) used)
0.61 0.07	U J (Ry)
0.61 0.07	U J (Ry)

---

nsic=0 for the AMF method (less strongly correlated electrons)

nsic=1 for the SIC method

nsic=2 for the HMF method

Review article : [E. R. Ylvisaker et al., Phys. Rev. B 79, 035103 \(2009\)](#)

## Input file case.ineece

On-site hybrid functional PBE0 applied to the 4f electrons of atoms No. 2 and 4:

---

-12.0	2	emin, natorb
2	1 3	iatom, nlorb, lorb
4	1 3	iatom, nlorb, lorb
HYBR		HYBR/EECE
0.25		fraction of exact exchange

---

# SCF cycle of DFT+ $U$ in WIEN2k

lapw0

$\rightarrow v_{xc,\sigma}^{\text{DFT}} + v_{ee} + v_{en}$  (case.vspup(dn), case.vnsup(dn))

orb -up

$\rightarrow v_{mm'}^{\uparrow}$  (case.vorbug)

orb -dn

$\rightarrow v_{mm'}^{\downarrow}$  (case.vorbdn)

lapw1 -up -orb

$\rightarrow \psi_{nk}^{\uparrow}, \epsilon_{nk}^{\uparrow}$  (case.vectorup, case.energyup)

lapw1 -dn -orb

$\rightarrow \psi_{nk}^{\downarrow}, \epsilon_{nk}^{\downarrow}$  (case.vectordn, case.energydn)

lapw2 -up

$\rightarrow \rho_{\text{val}}^{\uparrow}$  (case.clmvalup)

lapw2 -dn

$\rightarrow \rho_{\text{val}}^{\downarrow}$  (case.clmvaldn)

lapwdm -up

$\rightarrow n_{mm'}^{\uparrow}$  (case.dmatup)

lapwdm -dn

$\rightarrow n_{mm'}^{\downarrow}$  (case.dmatdn)

lcore -up

$\rightarrow \rho_{\text{core}}^{\uparrow}$  (case.clmcorup)

lcore -dn

$\rightarrow \rho_{\text{core}}^{\downarrow}$  (case.clmcordn)

mixer

$\rightarrow$  mixed  $\rho^{\sigma}$  and  $n_{mm'}^{\sigma}$

# Hybrid functionals

- ▶ **On-site** hybrid functionals can be applied only to localized electrons
- ▶ **Full** hybrid functionals are necessary (but expensive) for solids with delocalized electrons (e.g., in *sp*-semiconductors)

Two types of full hybrid functionals available in WIEN2k<sup>1</sup>:

- ▶ unscreened:

$$E_{\text{xc}} = E_{\text{xc}}^{\text{DFT}} + \alpha (E_{\text{x}}^{\text{HF}} - E_{\text{x}}^{\text{DFT}})$$

- ▶ screened (short-range),  $\frac{1}{|\mathbf{r}-\mathbf{r}'|} \rightarrow \frac{e^{-\lambda|\mathbf{r}-\mathbf{r}'|}}{|\mathbf{r}-\mathbf{r}'|}$ :

$$E_{\text{xc}} = E_{\text{xc}}^{\text{DFT}} + \alpha (E_{\text{x}}^{\text{SR-HF}} - E_{\text{x}}^{\text{SR-DFT}})$$

screening leads to faster convergence with  $\mathbf{k}$ -points sampling

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<sup>1</sup> F. Tran and P. Blaha, Phys. Rev. B 83, 235118 (2011)

## Hybrid functionals: technical details

- ▶ 10-1000 times more expensive than LDA/GGA
- ▶ **k**-point and MPI parallelization
- ▶ Approximations to speed up the calculations:
  - ▶ Reduced **k-mesh** for the HF potential. Example:  
For a calculation with a  $12 \times 12 \times 12$  **k**-mesh, the reduced **k**-mesh for the HF potential can be:  
 $6 \times 6 \times 6$ ,  $4 \times 4 \times 4$ ,  $3 \times 3 \times 3$ ,  $2 \times 2 \times 2$  or  $1 \times 1 \times 1$
  - ▶ Non-self-consistent calculation of the band structure
- ▶ Underlying functionals for unscreened and screened hybrid:
  - ▶ LDA
  - ▶ PBE
  - ▶ WC
  - ▶ PBESol
  - ▶ B3PW91
  - ▶ B3LYP
- ▶ Use `run_bandplothf_lapw` for band structure

## Hybrid functionals: input file case.inhf

Example for YS-PBE0 (similar to HSE06 from Heyd, Scuseria and Ernzerhof<sup>1</sup>)

---

0.25	fraction $\alpha$ of HF exchange
T	screened (T, YS-PBE0) or unscreened (F, PBE0)
0.165	screening parameter $\lambda$
20	number of bands for the 2nd Hamiltonian
6	GMAX
3	lmax for the expansion of orbitals
3	lmax for the product of two orbitals
1d-3	radial integrals below this value neglected

---

Important: The computational time will depend strongly on the number of bands, GMAX, lmax and the number of k-points

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<sup>1</sup> A. V. Krukau *et al.*, J. Chem. Phys. **125**, 224106 (2006)

# How to run hybrid functionals?

1. init\_lapw
2. Recommended: run(sp)\_lapw for the semilocal functional
3. save\_lapw
4. init\_hf\_lapw (this will create/modify input files)
  - 4.1 adjust `case.inhf` according to your needs
  - 4.2 reduced **k**-mesh for the HF potential? Yes or no
  - 4.3 specify the **k**-mesh
5. run(sp)\_lapw -hf (-redklist) (-diaghf) ...

# SCF cycle of hybrid functionals in WIEN2k

lapw0 -grr →  $v_x^{\text{DFT}}$  (case.r2v),  $\alpha E_x^{\text{DFT}}$  (:AEXSL)

lapw0 →  $v_{\text{xc}}^{\text{DFT}} + v_{\text{ee}} + v_{\text{en}}$  (case.vsp, case.vns)

lapw1 →  $\psi_{n\mathbf{k}}^{\text{DFT}}, \epsilon_{n\mathbf{k}}^{\text{DFT}}$  (case.vector, case.energy)

lapw2 →  $\sum_{n\mathbf{k}} \epsilon_{n\mathbf{k}}^{\text{DFT}}$  (:SLSUM)

hf →  $\psi_{n\mathbf{k}}, \epsilon_{n\mathbf{k}}$  (case.vectorhf, case.energyhf)

lapw2 -hf →  $\rho_{\text{val}}$  (case.clmval)

lcore →  $\rho_{\text{core}}$  (case.clmcor)

mixer → mixed  $\rho$

# Some recommendations

Before using a functional:

- ▶ read a few papers about the functional in order to know
  - ▶ for which properties or types of solids it is supposed to be reliable
  - ▶ if it is adapted to your problem
- ▶ figure out if you have enough computational resources
  - ▶ hybrid functionals and GW require (substantially) more computational resources (and patience)