

# Magnetism (FM, AFM, FSM)

### **Karlheinz Schwarz**

**Institute of Materials Chemistry TU Wien**







- In localized systems (e.g. some rare earth) the magnetism is mainly governed by the atom (Hund's rule)
- **In itinerant (delocalized) systems (many transition metals)** magnetism comes from partial occupation of states, which differ between spin-up and spin-down.
- Boarderline cases (some f-electron systems) details of the structure (e.g. lattice spacing) determine whether or not some electrons are localized or itinerant.



**Ferromagnetic (FM) (e.g. bcc Fe)**  $\oint \oint \oint \oint \oint \oint \oint \oint \oint$   $M > 0$ 

Antiferromagnetic (AFM) (e.g. Cr)

**M = 0** 

**Ferrimagnetic cases** 

the moments at different atoms are antiparallel but of different magnitude

 $\dot{\theta}$   $\dot{\theta}$   $\dot{\theta}$   $\dot{\theta}$   $\dot{\theta}$   $\dot{\theta}$   $\dot{\theta}$ **M > 0**

Non-collinear magnetism (NCM)

the magnetic moments are not ligned up parallel.

9999999







### Experimental facts:





- 1. The carriers of magnetism are the unsaturated spins in the d-band.
- 2. Effects of exchange are treated with a molecular field term.
- 3. One must conform to Fermi statistics.

Stoner, 1936





### In a

- non magnetic (NM) case  $N<sub>†</sub>$  **= N**<sub>↓</sub> (spin-up and spin-down)
- **ferromagnetic (FM) case**

 $N<sub>†</sub>$  **>**  $N<sub>⊥</sub>$  (majority and minority spin) the moments at all sites are parallel (collinear)

- the (spin) magnetic moment **m**
	- $m = N_{\uparrow} N_{\downarrow}$
	- its orientation with respect to the crystal axes is only defined by **spin orbit coupling**.
- **there can also be an orbital moment** it is often suppressed in 3d transition metals

$$
\chi = \frac{\chi_{\rm P}}{1-2\mu_{\rm B}^2 I_{\rm s}\mathcal{N}\left(\varepsilon_{\rm F}\right)}=\chi_{\rm P}\ S
$$

### Exchange splitting







- **The existence of ferromagnetism** (FM) is governed by the
- **Stoner criterion**

$$
I. N(E_F) > 1
$$

- $N(E_F)$  DOS at  $E_F$  (of NM case) Stoner parameter
	- ~ independent of structure
- **Ferromagnetism appears when the gain** in exchange energy is larger than the **loss** in kinetic energy







### Exchange splitting

### $E_F$  at high DOS

bcc Fe

# DFT ground state of iron





# Iron and its alloys











### V. Heine: "metals are systems with unsaturated covalent bonds"











## ■ e.g. Fe-Co alloys

**Nigner delay times** 



## Spin projected DOS of Fe-Co alloys









### Itinerant or localized?

**Magnetization density** difference between



- **Majoity spin**
- **Minority spin**







### **Magnetization density** difference between

- **Majoity spin**
- **Minority spin**

 $m(r) = \rho^{\dagger}(r) - \rho^{\dagger}(r)$ 

### **Localized around**

- **Fe and Co**
- **slightly negative** between the atoms

### **Itinerant electrons**

K.Schwarz, P.Mohn, P.Blaha, J.Kübler, Electronic and magnetic structure of bcc Fe-Co alloys from band theory, J.Phys.F:Met.Phys. **14**, 2659 (1984)



# Bonding by Wigner delay time



$$
V(r) = \begin{cases} V(r) & r \leq b, \\ 0 & r > b. \end{cases}
$$
 (1)

Inside such a sphere of radius  $b$  the radial Schrödinger equation (in Rydberg atomic units)

$$
-\frac{d^2}{dr^2}-\frac{2}{r}\frac{d}{dr}+\frac{l(l+1)}{r^2}+V(r)-\varepsilon\bigg]R_l(\varepsilon,r)=0,
$$
\n(2)

single scatterer (Friedel)

 $V(r)$ 

R

 $V(r)=0$  solution:

 $R<sub>l</sub>$  joined in value and slope defines phase shift :

Friedel sum

Wigner delay time

Bessel Neumann  
\n
$$
S_{i}(r) = A_{i}[j_{i}(kr)\cos \eta_{i}(\varepsilon) - n_{i}(kr)\sin \eta_{i}(\varepsilon)], \qquad (3)
$$

$$
\tan \eta_l(\varepsilon) = \frac{R_l(\varepsilon, b) j'_l(kb) - j_l(kb) R'_l(\varepsilon, b)}{R_l(\varepsilon, b) n'_l(kb) - n_l(kb) R'_l(\varepsilon, b)}, \qquad (4)
$$

$$
N(\varepsilon) = \frac{2}{\pi} \sum_{l=0}^{\infty} (2l+1) \eta_l(\varepsilon),
$$
  
\n
$$
n(\varepsilon) = \frac{dN(\varepsilon)}{d\varepsilon} = \frac{1}{\pi} \sum_{l=0}^{\infty} (2l+1) t_l^{\rm D}(\varepsilon).
$$
 (6)

















 $-8$ 

 $-1.2$ 

 $\ddot{q}$ 

 $0.4$ 

 $0.8$ 

 $\overline{9}$ 

 $\overline{12}$ 

 $0.0$ 

 $\left[\frac{1}{2} \text{mod } 2 \text{ mod } 2 \$ 

### Covalent magnetism, FeCo:







### Cr has AFM bcc structure



- **There is a symmetry** 
	- it is enough to do the spin-up calculation
	- spin-down can be copied

$$
Cr_1^{\frac{1}{2}} = Cr_2^{\frac{1}{2}}
$$
  
Cr<sub>2</sub> = Cr<sub>1</sub>



### **Al-silicate**

- **CORNER** shared
	- $S$ iO<sub>4</sub> tetrahedra
	- $\blacksquare$  AlO<sub>4</sub> tetrahedra
- $\blacksquare$  β cage
- **Al / Si ratio 1**
- **alternating**
- ordered (cubic)
- 3 e<sup>-</sup> per cage







- **Si-Al zeolite (sodalite)** 
	- Formed by corner-shared  $SiO<sub>4</sub>$ and AIO<sub>4</sub> tetrahedra
- Charge compensated by doping with
	- $\blacksquare$  4 Na<sup>+</sup>
	- one e<sup>-</sup> (color center)
- antiferromagnetic (AFM) order of e-



Energy (relative stability)







### AFM order between color centers (e<sup>-</sup>)

Spin density 
$$
ρ
$$
<sup>↑</sup> -  $ρ$ <sup>↓</sup>





G.K.H. Madsen, Bo B. Iversen, P. Blaha, K. Schwarz, Phys. Rev. B 64, 195102 (2001)





### e.g. Fe-Ni

**Such systems essentially show** no thermal expansion around room temperature







- **The thermal expansion of the Eifel tower**
- **Measured with a rigid Fe-Ni INVAR wire**
- **The length of the tower correlates with** the temperature
- **Fe<sub>65</sub>Ni<sub>35</sub>** alloy has vanishing thermal expansion around room temperature





### What is magnetostriction?

Magnetostriction  $\omega_{s0}$  is the difference in volume between the volume in the magnetic ground state and the volume in a hypothetical non-magnetic state.

Above the Curie temperature the magnetic contribution  $\omega_{\rm m}$  vanishes.







### "classical" Fe-Ni Invar



**Fe<sub>65</sub>Ni<sub>35</sub>** alloy has vanishing thermal

# Early explanations of INVAR





A.R.Williams, V.L.Moruzzi, G.D.Gelatt Jr., J.Kübler, K.Schwarz, Aspects of transition metal magnetism, J.Appl.Phys. **53**, 2019 (1982)

# Energy surfaces of Fe-Ni alloys



- **This fcc structure** 
	- from non magnetic Fe (fcc)
	- to ferromagnetic Ni
	- as the composition changes
- **At the INVAR composition** 
	- There is a flat energy surface
		- as function of volume and moment







### Energy surface at  $T=0$  (DFT)

- as a function of volume and moment
- using fixed spin moment (FSM) calculations
- **Finite temperature** 
	- Spin and volume fluctuations
	- Ginzburg-Landau model

$$
H = V^{-1} \int d^{3}r (E(M + m(r)), V + v(r)) + \frac{C}{2} \sum_{i,j} (\nabla_{j}m_{i})^{2} + \frac{D}{2} (\nabla v(r))^{2})
$$







# **Fixed spin moment (FSM)** e.g. Fe-Ni alloy

- allows to explore energy surface  $E(V,M)$ as function of
	- volume V
	- magnetic moment M

# Fixed spin moment (FSM) method



- **There are systems (e.g. like fcc Fe** or fcc Co), for which the magnetization shows a hysteresis, when a magnetic field is applied (at a volume V).
- **The volume of the unit cell defines** the Wigner-Seitz radius  $r_{WS}$

$$
V=\frac{4\pi r_{WS}^3}{3}
$$

- **The hysteresis causes numerical** difficulties, since there are several solutions (in the present case 3 for a certain field H).
- In order to solve this problem the FSM method was invented











### **Physical situation:**

- One applies a field H and obtains M
- **p** but this functions can be multivalued

- Computational trick (unphysical):
	- One interchanges the dependent and independent variable
	- this function is single valued (unique)
	- **.** *i.e. one chooses M and calculates* H afterwards











A.R.Williams, V.L.Moruzzi, J.Kübler, K.Schwarz, Bull.Am.Phys.Soc. **29**, 278 (1984)

K.Schwarz, P.Mohn J.Phys.F **14**, L129 (1984)

P.H.Dederichs, S.Blügel, R.Zoller, H.Akai, Phys. Rev, Lett. **53**,2512 (1984)





# ■ GMR (Giant Magneto Resistance)

# half-metallic systems e.g.  $CrO<sub>2</sub>$

**n** important for spintronics





Once upon a time, in the early 1980's …



### Peter Grünberg



The electrical resistance depends on the relative magnetic alignment of the ferromagnetic layers

$$
GMR = \frac{R_{AP} - R_P}{R_P}
$$

19% for trilayers @RT 80% for multilayers @ RT

GMR is much larger than the anisotropic magnetoresistance (AMR)



R<sub>AP</sub>

# 1988: … simultaneously, but independent …



"Does the electrical resistance depend on the magnetization alignment?"





Albert Fert



### Peter Grünberg







#### The Nobel Prize in Physics 2007



techniques for retrieving data from hard disks.

Scientific Background on the Nobel Prize in Physics 2007

### The Discovery of Giant Magnetoresistance

compiled by the Class for Physics of the Royal Swedish Academy of Sciences

#### 4. Half-metals

Since magnetoresistance deals with electrical conductivity it is obvious that it is the behaviour of the electrons at the Femi surface (defined by the Fermi energy) which is of primary interest. The more spin-polarized the density of states (DOS) at the Fermi energy, i.e., the more  $N_{\uparrow}$  (E<sub>F</sub>) deviates from  $N_{\downarrow}$  $(E_F)$ , the more pronounced one expects the efficiency of the magnetoelectronic effects to be. In this respect a very interesting class of materials consists of what are called half-metals, a concept introduced by de Groot and co-workers (23). Such a property was then predicted theoretically for  $CrO<sub>2</sub>$  by Schwarz in 1986 (24). The name half-metal originates from the particular feature that the spin down band is metallic while the spin up band is an insulator.

K. Schwarz, "CrO<sub>2</sub> predicted as a half-metallic ferromagnet", J. Phys. F, 16, L211 (1986). 24.

<http://www.kva.se/>

Scientific background



important for spintronics



 $\blacksquare$  The DOS features of CrO<sub>2</sub> are qualitatively like

K.Schwarz,  $CrO<sub>2</sub>$  predicted as a half-metallic ferromagnet, J.Phys.F:Met.Phys. **16**, L211 (1986)



all three compound crystallize in the rutile structure







### $Cro<sub>2</sub>$  (rutile structure)



# CrO<sub>2</sub> spin-down (**TiO<sub>2</sub>**) spin-up (**RuO<sub>2</sub>**)







# Magnetic structure of uranium dioxide  $UO<sub>2</sub>$



- R.Laskowski
- G.K.H.Madsen
- P.Blaha
- K.Schwarz





### **topics**

- non-collinear magnetism
- spin-orbit coupling
- $\blacksquare$  LDA+U (correlation of U-5f electrons)
- Structure relaxations
- electric field gradient (EFG)



R.Laskowski, G.K.H.Madsen, P.Blaha, K.Schwarz: Magnetic structure and electric-field gradients of uranium dioxide: An ab initio study Phys.Rev.B **69**, 140408-1-4 (2004)

# Atomic configuration of uranium  $(Z=92)$







### non-collinear magnetism in  $UO<sub>2</sub>$







## UO2 2k structure, LDA+SO+U





- **Magnetisation** direction perpenticular at the two U sites (arrows)
- **Magnetisation** density (color)







• Wien2k can only handle collinear or non-magnetic cases







runsp lapw script (unconstrained magnetic calc.)

- runs lapw1/2 for both spins independently
- case scf contains extra information:
	- grep : MMT case.scf (for total moment)
	- grep : MMI case.scf (for atomic moments)
	- grep : HFF case.scf (for hyperfine fields)





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		- grep : HFF case.scf (for hyperfine fields)
- runfsm lapw -m value (constrained moment calc.)
	- for difficult to converge magnetic cases or simply to constrain a<br>moment (-> 2 Fermi-energies -> external magnetic field)
- $runafm \; \lambda$  Lapw (anti-ferromagnetic calculation)
	- calculates only spin-up, uses symmetry to generate spin-dn





- runsp lapw script (unconstrained magnetic calc.)
- runfsm lapw -m value (constrained moment calc.)
- runafm lapw (anti-ferromagnetic calculation)

- spin-orbit coupling can be included in second variational step
- never mix polarized and non-polarized calculations in one case directory !!!



## Thank you for your attention



